

AMI Simulation with Error Correction to Enhance BER Performance

10-WP6

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Agenda

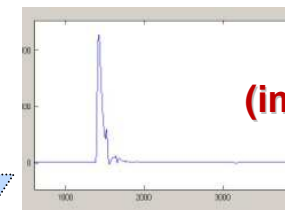
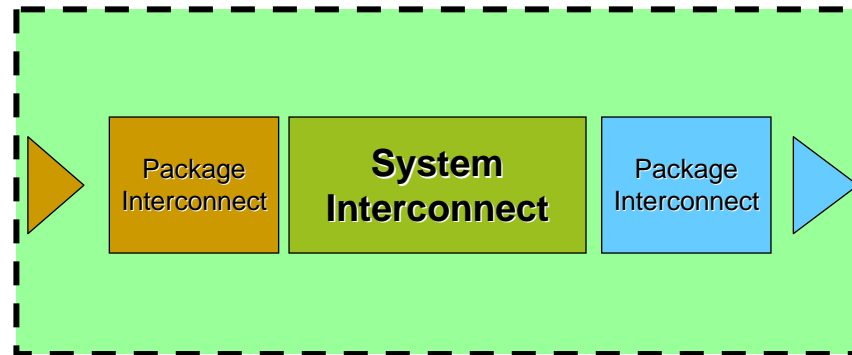
- Overview
- Serial link simulation process
- IBIS-AMI modeling
- Error correction theory and methods
- Prediction of BER improvement with FEC

Overview

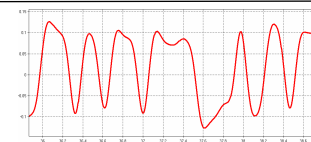
- IBIS 5.0 introduced Algorithmic Modeling Interface (AMI) for modeling advanced SerDes EQs like DFE
- DFE model operation can provide key insight into burst errors that can degrade BER
- Error correction methods have historically been used for optical links
- These methods can also be applied to electrical serial link interfaces to enhance BER
- This paper examines FEC application to serial link simulation, leveraging information from AMI simulations using adaptive DFE models

Serial Link Simulation Process

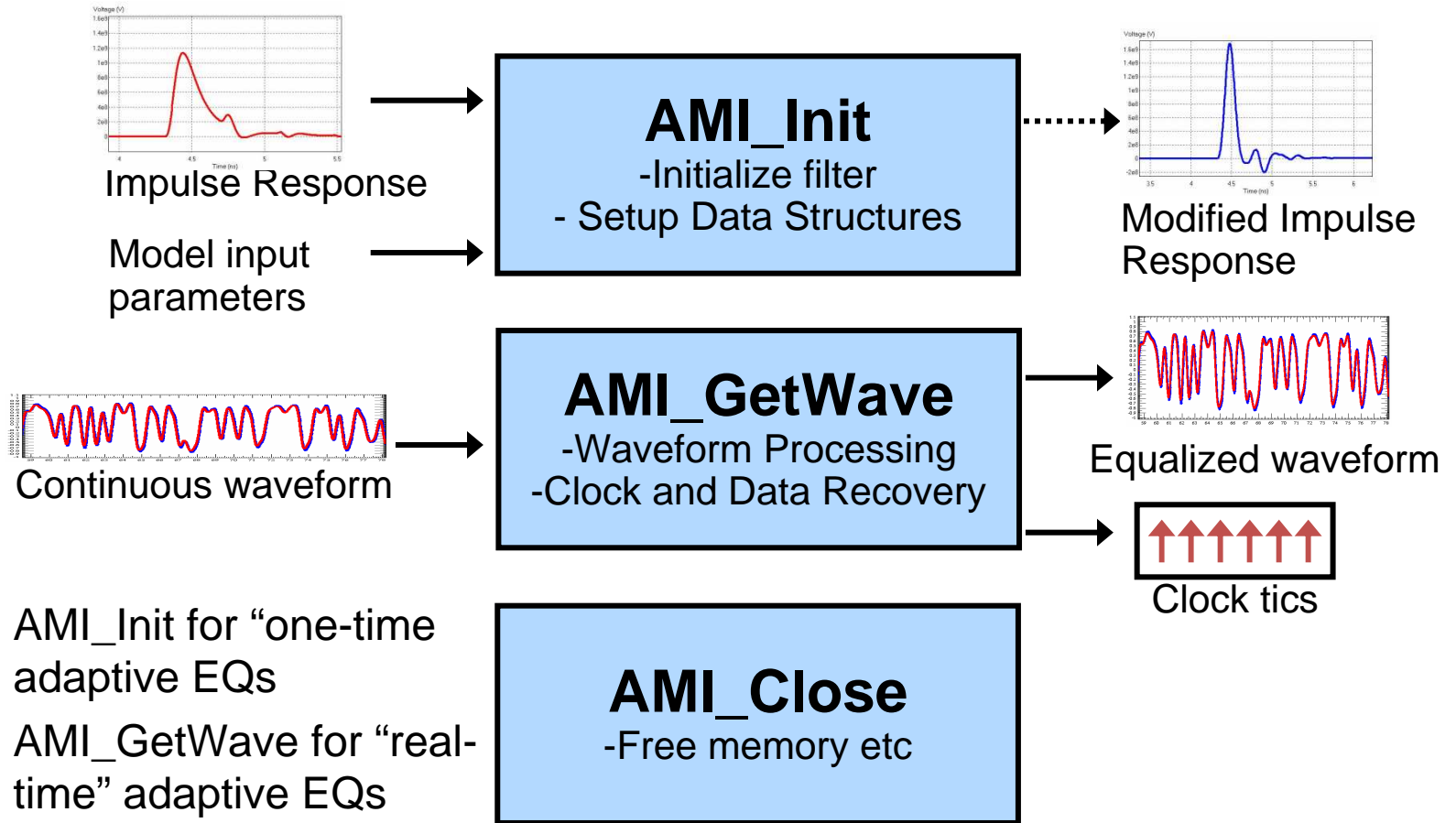
- Analog channel is exercised in Spice to produce an impulse response
- Impulse response is convolved with the bit stream to produce raw waveforms



(impulse response)

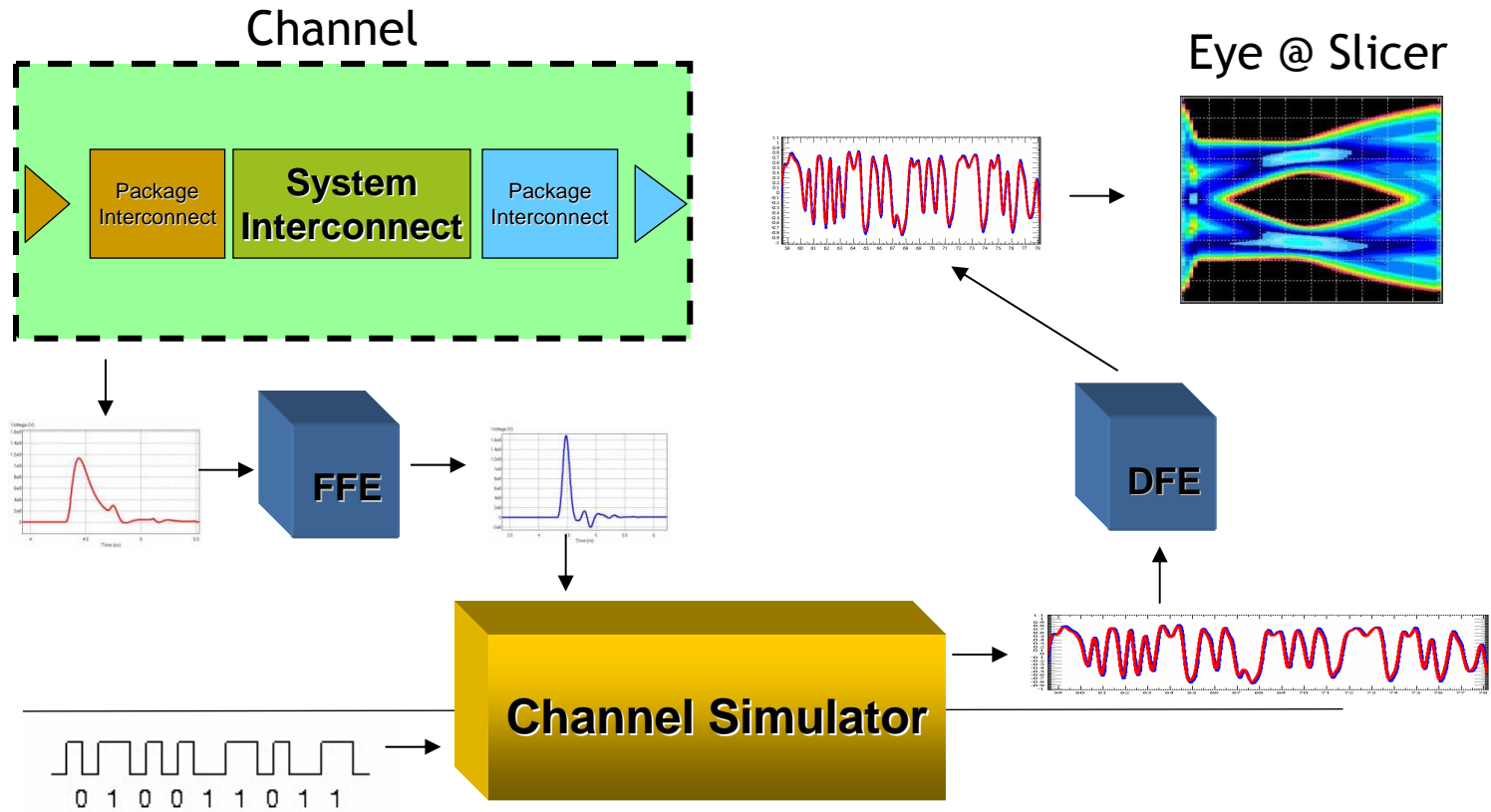


APIs in IBIS-AMI Modeling



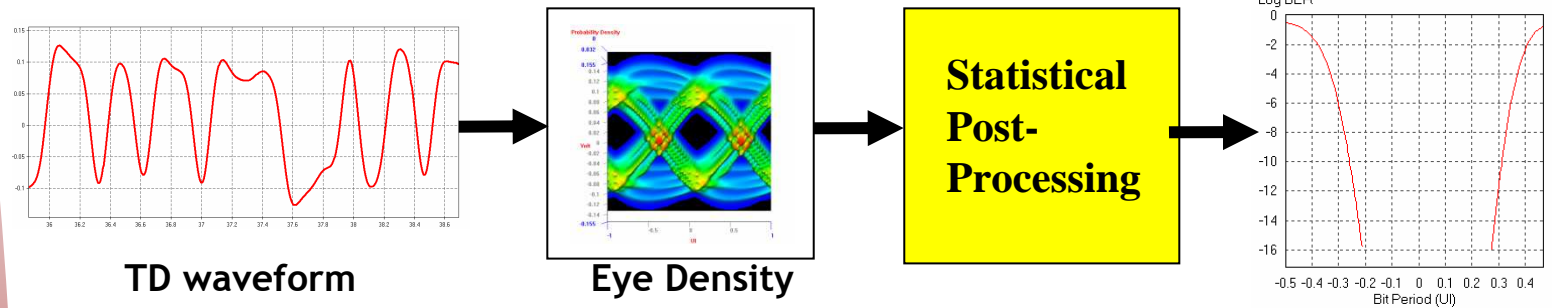
- AMI_Init for “one-time adaptive EQs
- AMI_GetWave for “real-time” adaptive EQs

IBIS-AMI in Channel Simulation



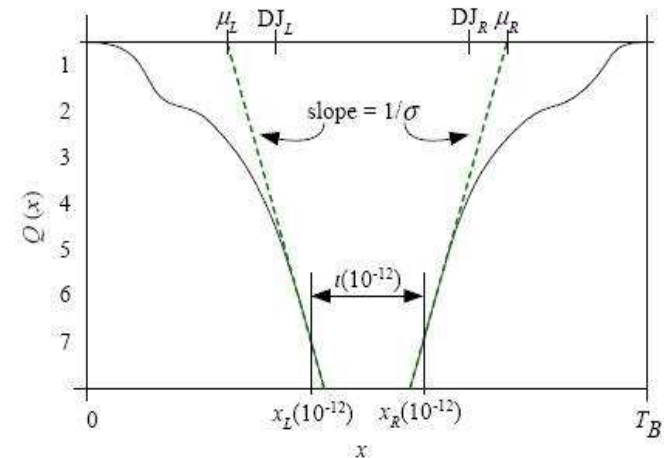
Bathtub Curve Generation

- Waveforms are used to determine the eye density
- Eye density is post-processed to produce bathtubs



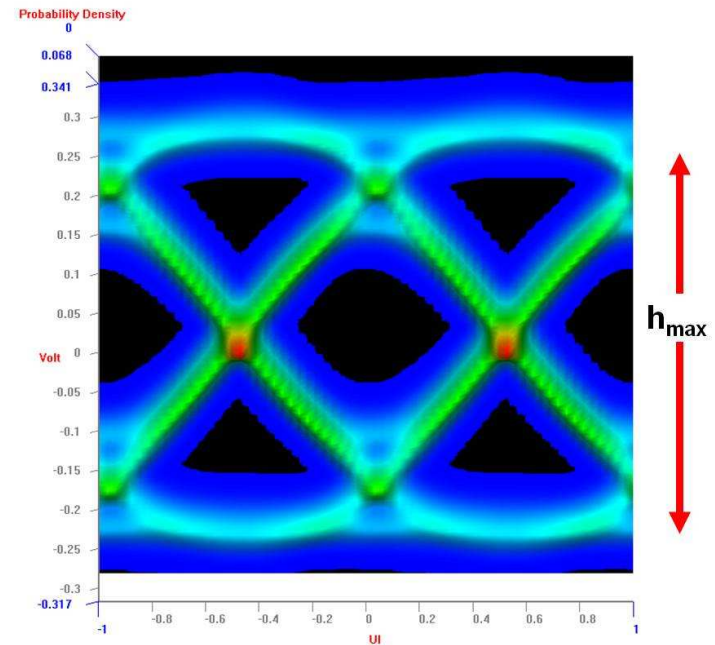
Dual Dirac Method is used for statistical post-processing:

- Extrapolated “cumulative eye distribution” at center
- Based on Gaussian tail extrapolation
- Intersection is proportional to D_j
- Slope represents R_j



Weighted Eye

- Metric to quantify the sparseness of the eye distribution
- Sparser eye is better BER
- “hmax” is the eye height at the outer envelope, used for normalization
- Excellent means to quantify the effect of equalization, as well as the effect of the various components that comprise the channel



$$\text{Weighted_eye} = \sum h(y)p(y)$$

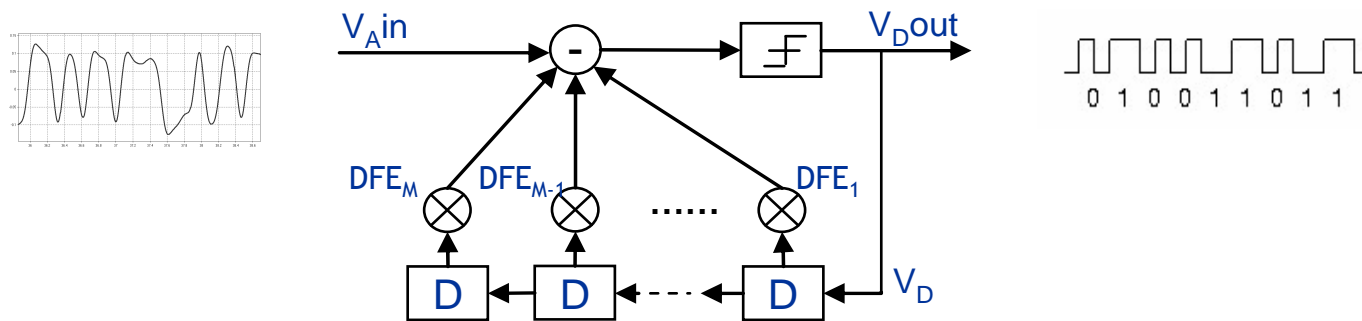
$h(y)$ - eye height

$p(y)$ - probability

Error Mechanism in High Speed Serial Link

High speed serial links have a mixed error mechanism, random and burst errors.

- DFE can introduce burst errors due to the feedback mechanism



$$V_{Dout}(t_0) = \text{sign}(V_{Ain}(t_0) - DFE_1 \cdot V_D(t_{-1}) - DFE_2 \cdot V_D(t_{-2}) - \dots - DFE_M \cdot V_D(t_{-M}))$$

$$\text{sign}(x) = \begin{cases} 1, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

- Once errors occur, they change the output voltage and thus impact the judgments of the equalized bits that follow. A “domino effect” can result

Error Propagation Calculation Methods (1)

- Error propagation is modeled by probability calculation^[3]:

$$BER = \sum_{i=1}^{rll_{\max}} \sum_{all E} p(rll = i, E) \cdot W(E) \cdot p_1 \cdot (1 - p_1)^{n - rll_{\max} - i}$$

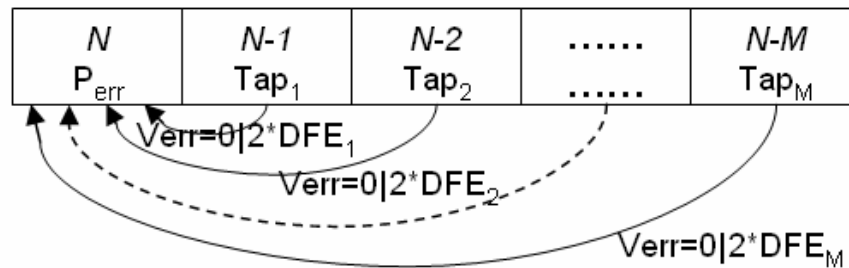
Diagram illustrating the components of the BER equation:

- rll_{\max} : maximum error propagation length
- $\sum_{all E}$: all the combinations of the error pattern when error propagation length is i
- $p(rll = i, E)$: the probability that i bits in error among a n bit block
- $W(E)$: random error probability
- p_1 : random error probability
- $(1 - p_1)^{n - rll_{\max} - i}$: random error probability

- A critical aspect in estimating BER with error propagation is to calculate the probabilities of erroneous bits due to different propagation lengths: $p(rll = 1 : rll_{\max})$

Error Propagation Calculation Methods (2)

- The probabilities are gleaned from the raw voltage bathtub curves, by calculating the probabilities of error pattern E



- The voltage offset from a feedback loop is represented by

$$[V_{sum_err_j} | p_j] = \sum_{i=1}^M Verr(i)$$

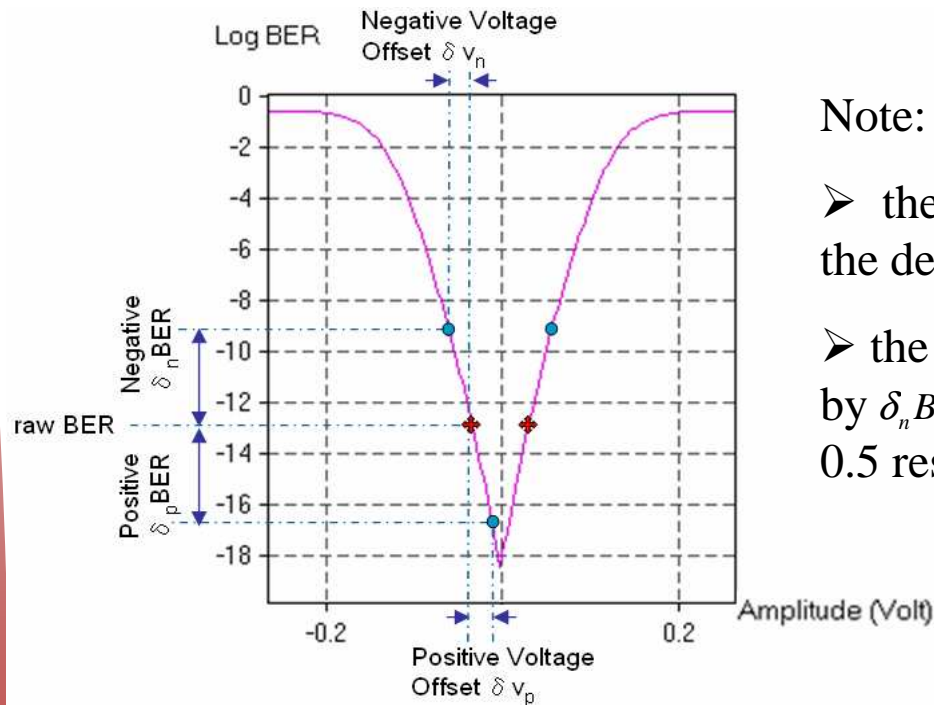
When i th bit error, $Verr(i) = 2 \cdot DFE(i)$ else $Verr(i) = 0$

$$p_j = \prod_{i=1}^{2^M} [p_i | (1-p_i)]$$

When i th bit error using p_i else $(1-p_i)$

Error Propagation Calculation Methods (3)

- A certain voltage offset due to wrong judgment can be estimated and BER due to this offset can be obtained directly from the bathtub curve.



Note:

- the diamond markers are located at the decision slicer levels
- the raw BER degrades or improves by $\delta_n BER$ or $\delta_p BER$ at the probability of 0.5 respectively.

- The BER due to error propagation should be the mean value of the BERs taken from the left and right bathtub curves.

Enhancing BER with Error Correction (1)

Assuming:

Err_DFE is the probability vector of a burst length, and contains rl probability values

Err_rand is the random error rate

N is the packet length

The total BER including the error propagation is calculated by

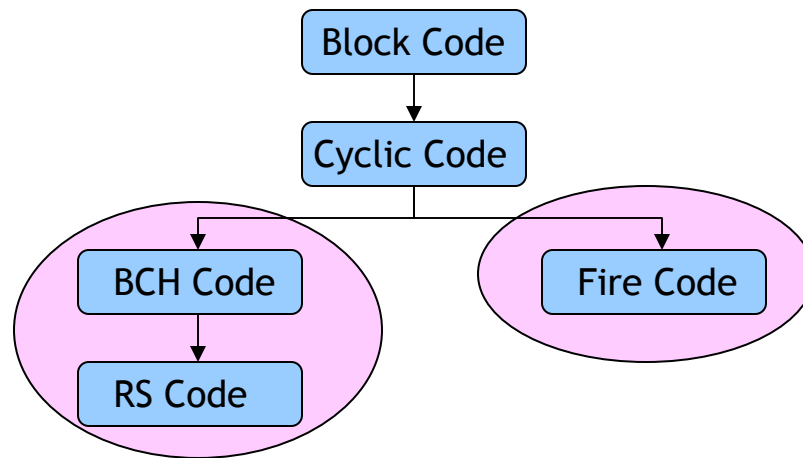
$$BER_{total} = \frac{1}{N} \sum_{allP} \sum_{i=0}^H P_{pkt}(i+1|i)$$

- a function of the vector Err_DFE .
- The $(i+1)th$ burst error rate in a packet under the condition that the ith burst error occurs in the same packet
- When i equals to 0, P_{pkt} is simply the probability vector of the 1st burst error in the packet.

- Note that H is a customized number that is determined by Err_DFE , and the value of H should be picked by the user.
- Different probability levels can be subtracted from BER_{total} to get the enhanced BER values.

Enhancing BER with Error Correction (2)

Common error correction codes: block codes and convolution codes

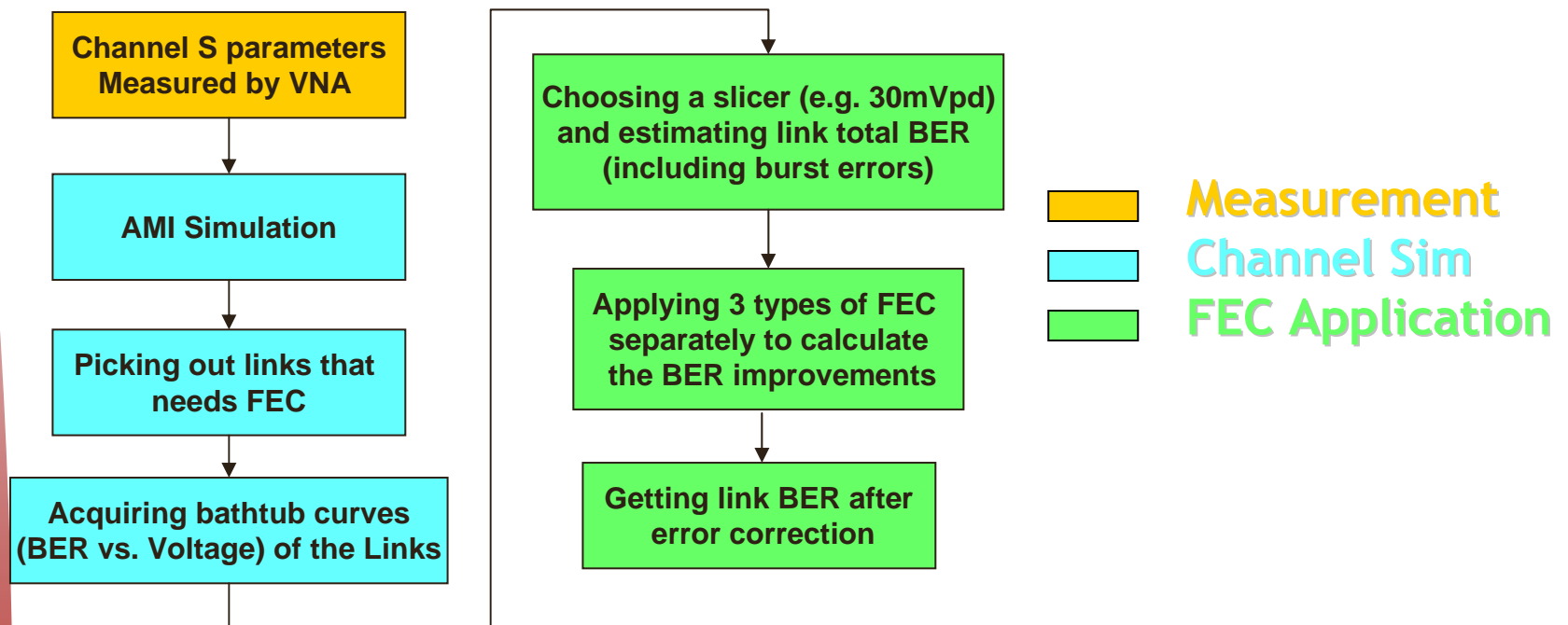


In the following experiment, 3 kinds of block codes are interested:

1. BCH codes that deal with random errors
2. Fire codes that deal with single burst errors (burst length with 7 and 11 bits are investigated separately)
3. RS code that can deal with multiple burst errors (8-symbol errors are considered)

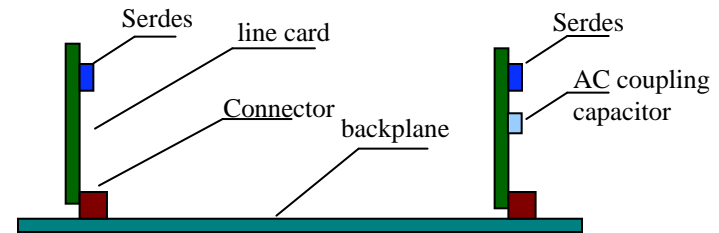
AMI Simulation Flow Incorporated with FEC

The following flow was utilized in the case study:

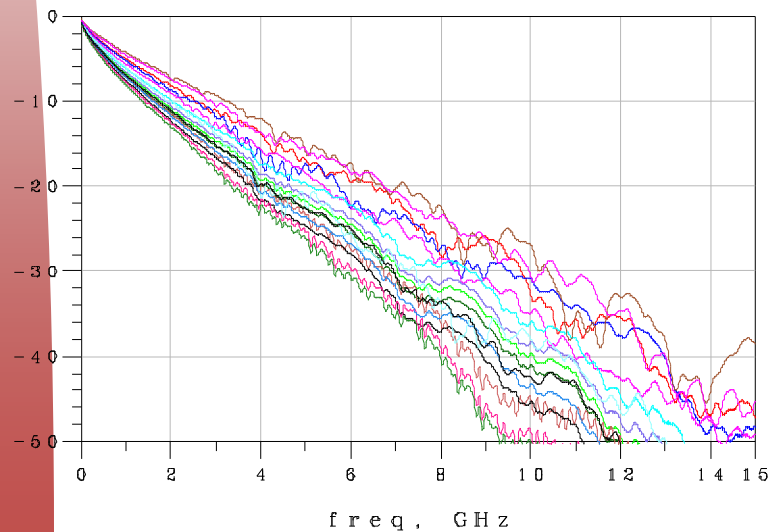


System Configuration

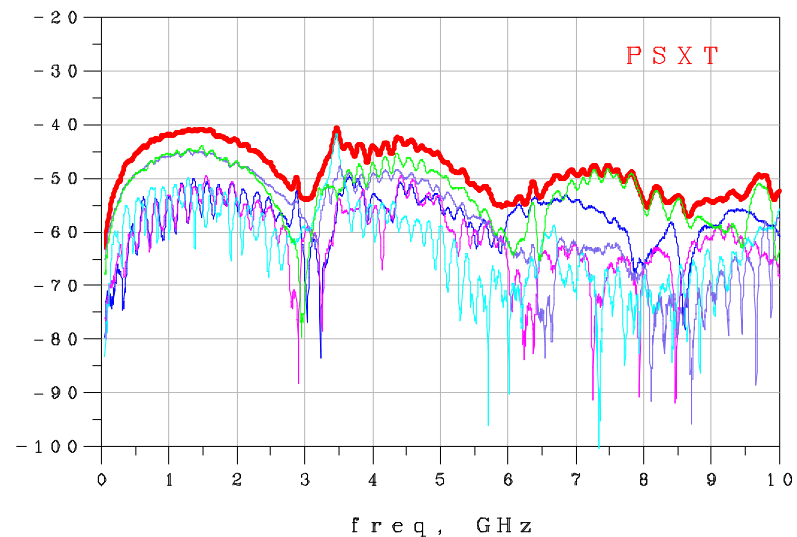
- SerDes IP: HSS12, Worst case, 3-tap emphasis and 5-tap DFE
- SerDes package: User defined
- Data Rate: 10.3125Gbps
- Coding: PRBS23+64B/66B
- Target BER: 1e-17
- Simulation bit number: 2000000
- Channel: Experimental backplane system, with 5 crosstalk channels



Insertion Loss (dB) vs Frequency (GHz)

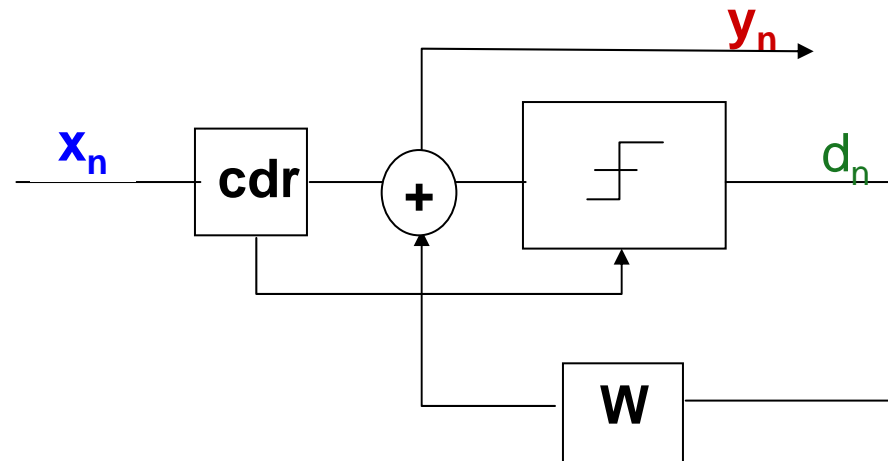


PSXT (dB) vs Frequency (GHz)



IBM HSS12 Rx AMI Model

- Multi-phase, 5-tap Decision Feedback Equalizer (DFE)
- Integrated CDR (clock/data recovery)
- Real time, adaptive equalization
- Signal processing of time domain waveforms

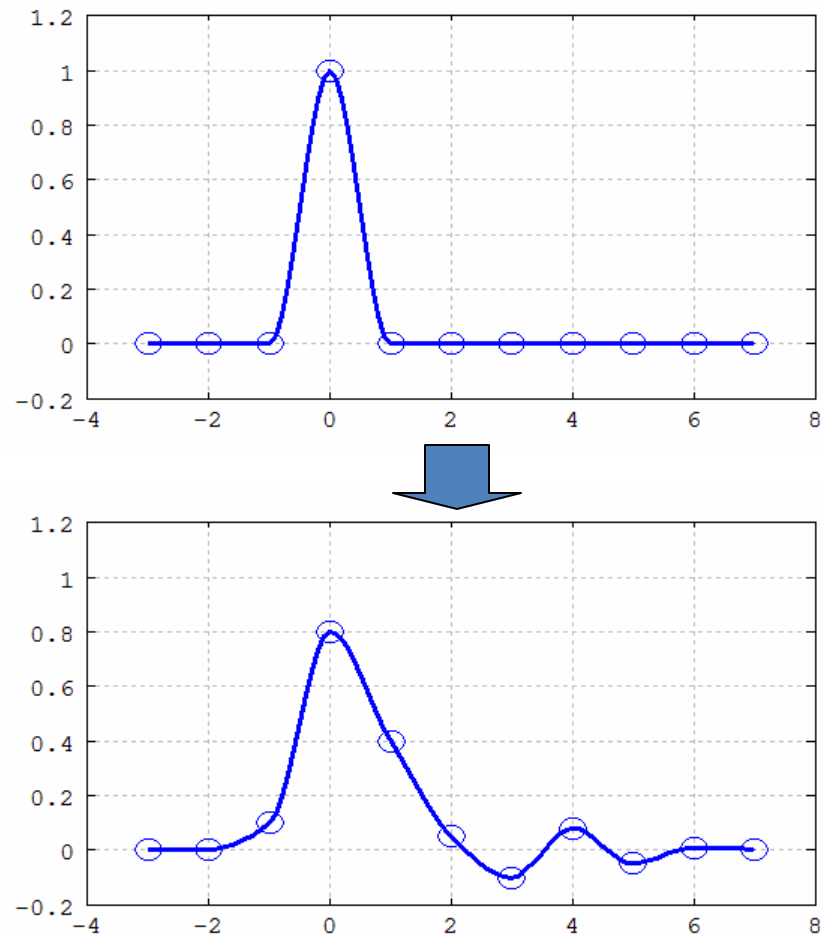


$$y_n = x_n + \sum w_i * d_i$$

y_n - output
 x_n - input
 d_i - previous 'i_{th}' decision
 w_i - i_{th} tap weight

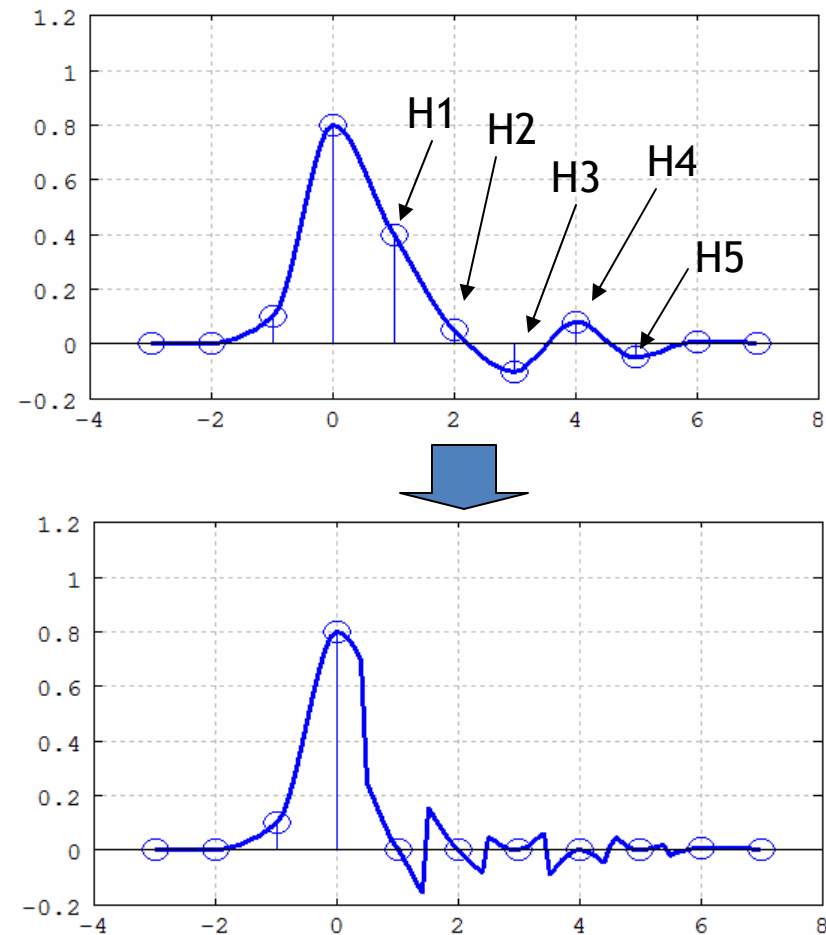
Decision Feedback Equalization (1)

- Inter-Symbol Interference (ISI) introduced by channel
- Each bit's signal value influences the following few bits
- DFE compensates for a 'decided' value
- IBM HSS12 Rx, 5-tap DFE used



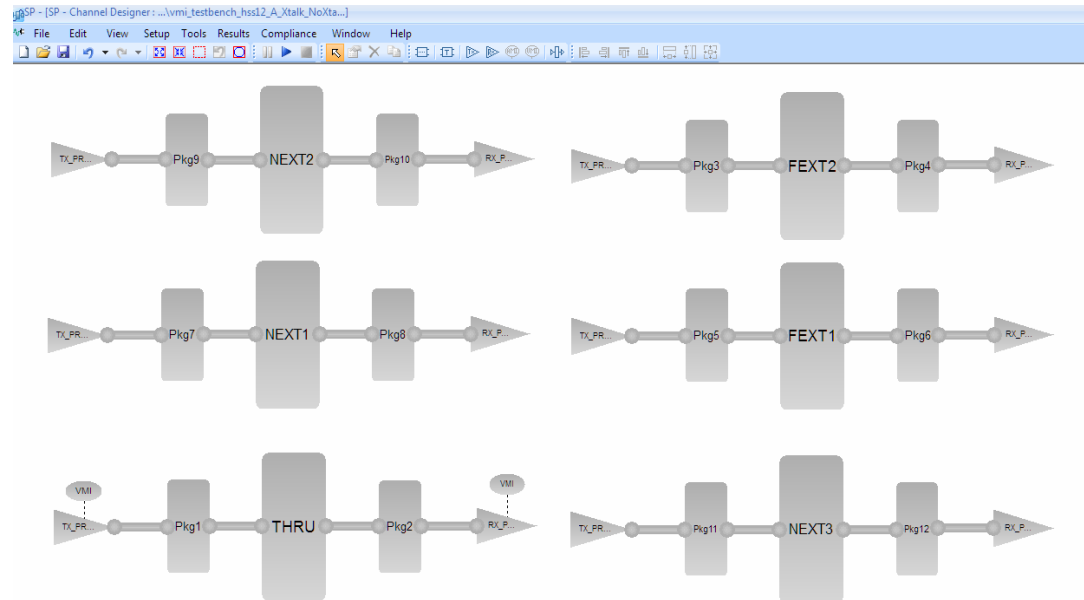
Decision Feedback Equalization (2)

- DFE adds weighted +/- value of previous 5 bits
- Weights determined by adaptation/feedback
- H1 decision 'speculative'
- Pre-cursor ISI not affected
- ISI reduction dependent on 'decision' being correct!



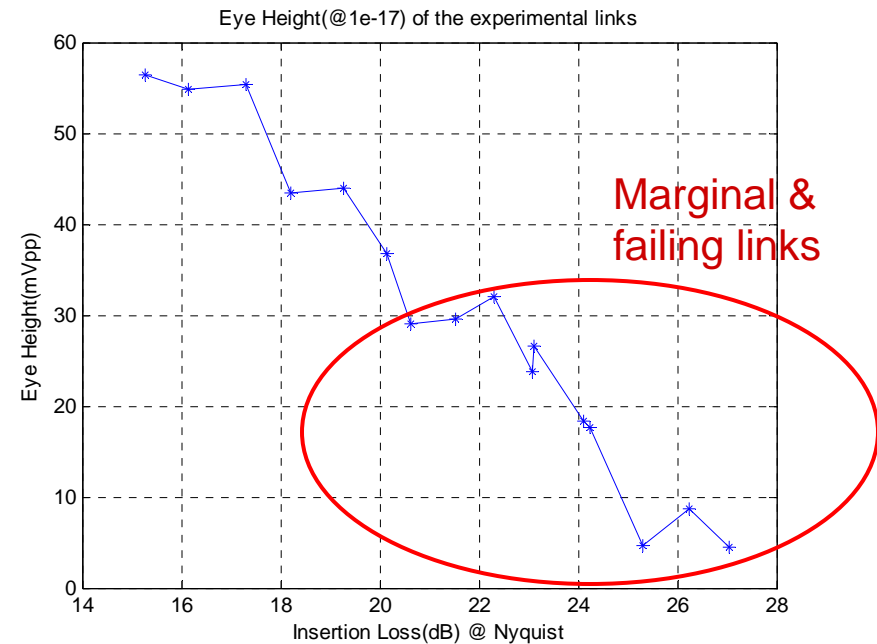
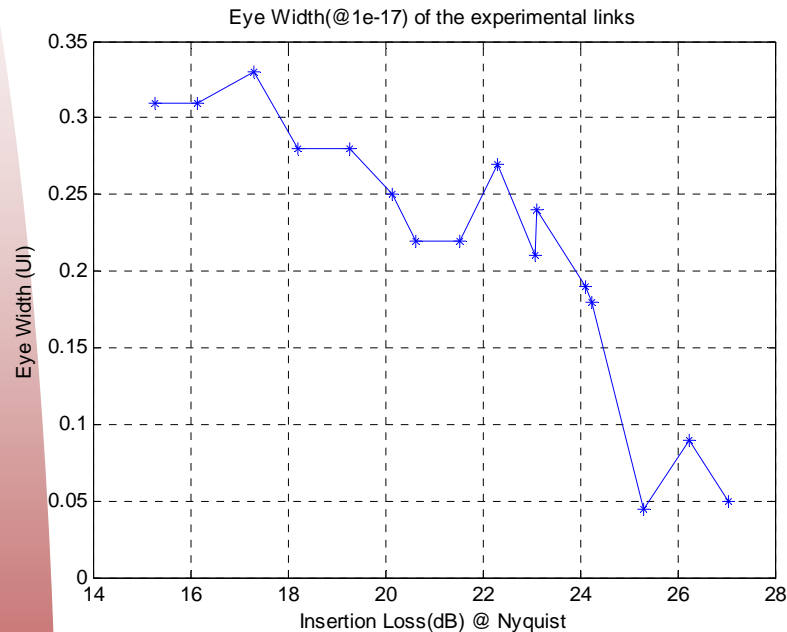
Simulation Topology

- “Through” channel with multiple crosstalk channels
 - 3 “NEXT” near-end crosstalk
 - 2 “FEXT” far-end crosstalk
- All channels taken from measured S-parameters



- Through channel swept for insertion loss of 15 to 30dB (at 5GHz)
- IBM IBIS-AMI models for Tx and Rx

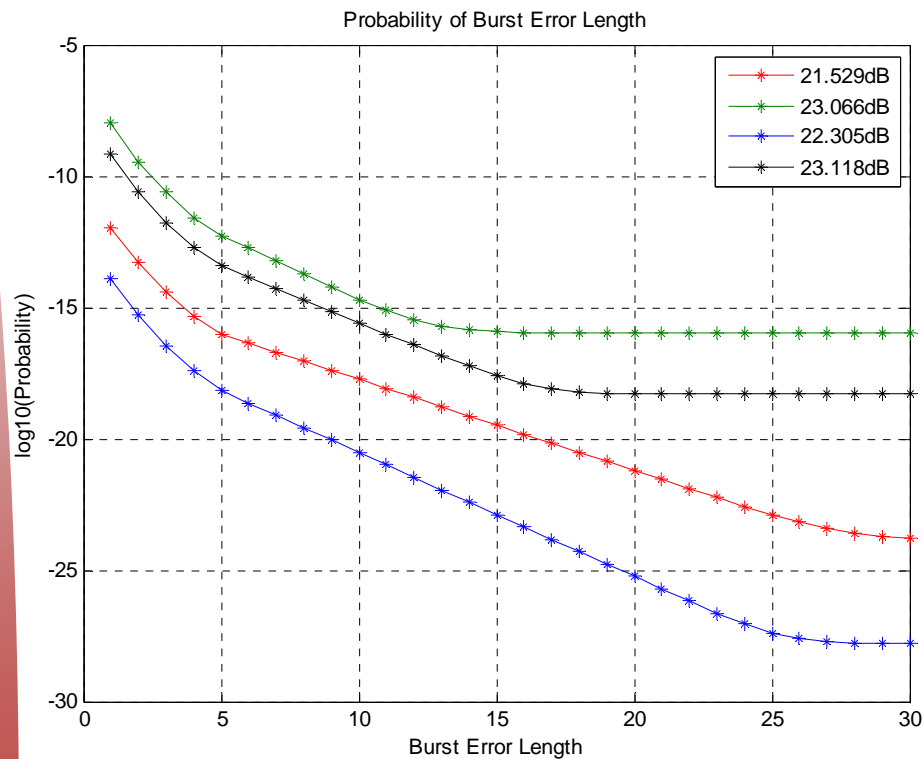
Link Margin Identification



- Requirements for IBM HSS12 core:
 - 10~15% UI of horizontal eye opening
 - 20~30mVpd of vertical eye opening required
- 10 out of 16 channels were deemed “marginal” or failing and selected for FEC

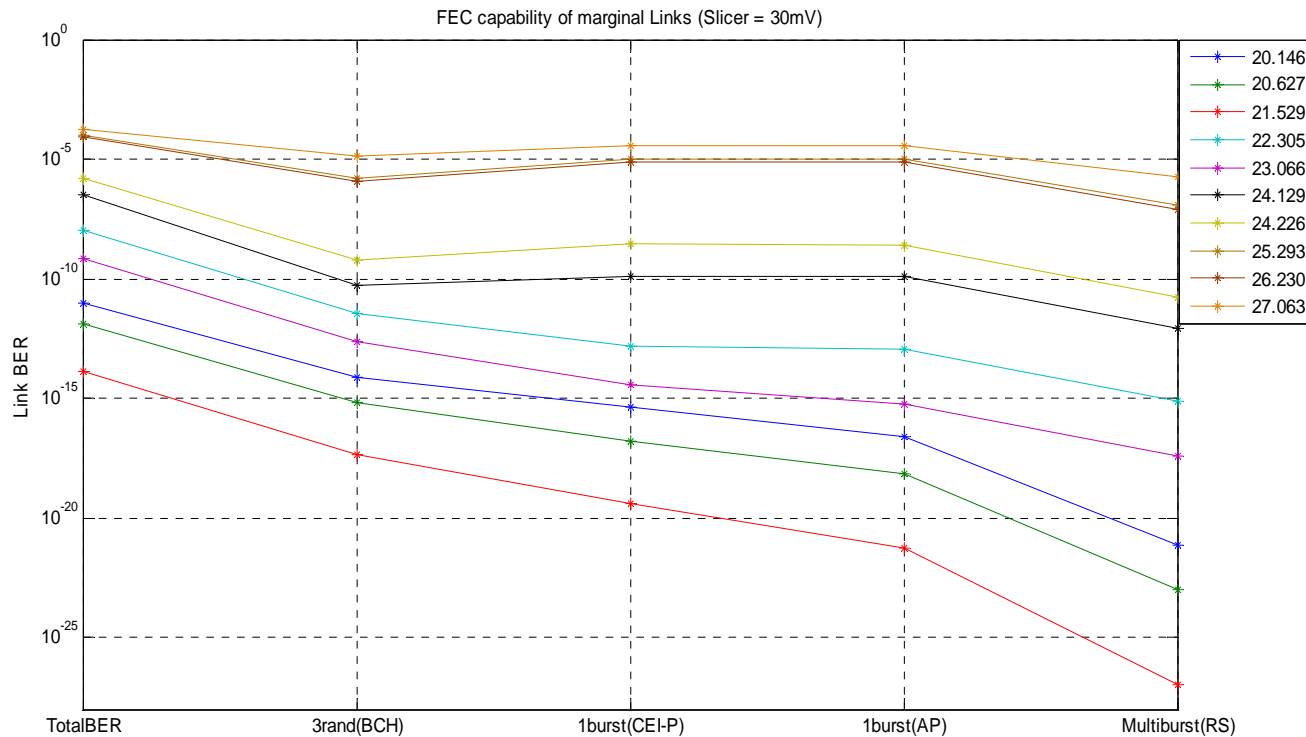
Error Propagation Calculation

Error propagation probabilities of 4 sample links:



➤ Note that the error propagation probability levels are not only related to the DFE coefficients, but also related to the error nature of the links.

BER Enhancement



- The 3-random correcting BCH can improve the BER approximately by 10^3 ;
- The 1-burst error correcting Fire codes can improve the BER by at least 10^4 ;
- The RS code (correcting 8 symbols) can achieve a BER enhancement of 10^8 .

Summary

- A methodology has been presented to quantify BER improvement of electrical serial links, using error correction codes (FEC)
- Proof-of-concept has been achieved on an experimental Huawei backplane system
- Standard IBIS-AMI modeling and simulation can be used as the basis of this analysis
- FEC has shown capability to improve BER performance for marginal serial links

References

- [1] Ransom Stephens, “Jitter analysis: The Dual-Dirac Model, RJ/DJ, and Q-scale, Version 1.0”, Agilent Technologies, 31-December-2004.
- [2] Mike Peng Li, Jitter, Noise and Signal Integrity at High-Speed, Prentice Hall 2008.
- [3] Cathy Ye Liu and Joe Caroselli, “Modeling and Mitigation of Error Propagation of Decision Feedback Equalization in High Speed Backplane Transceivers.” Proceedings of DesignCon 2006.
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- [5] Shu Lin and Daniel J. Costello, Error Control Coding: Fundamentals and Applications, Prentice Hall, 2002.
- [6] IBM, “HSSCDR User’s Guide”, 2008.